

Philosophy 405: Knowledge, Truth and Mathematics
Spring 2008
M, W: 1-2:15pm

Hamilton College
Russell Marcus
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Schedule

Class 1: What is mathematics? What is philosophy of mathematics? (1/21)

Readings:

Brown, Chapter 1
Shapiro, pp 21-29

Class 2: Pythagoras and the Pythagoreans (1/23)

Primary Readings

Kline, "The Creation of Classical Greek Mathematics"
Kline, "The Greek Rationalization of Nature"

Class 3: Plato's Platonism (1/28)

Seminar Paper 1: Jazmine
Seminar Paper 2: Jonathan
Primary Readings

Selections from Plato on Mathematics

Secondary Readings

Shapiro, pp 49-63
Brown, Chapter 2

Class 4: Aristotle (1/30)

Seminar Paper 1: Nelson
Seminar Paper 2: Walter
Primary Reading

Aristotle, "Books XIII and XIV"

Secondary Reading

Shapiro, pp 63-71

Class 5: Modern rationalism I (2/4)

Seminar Paper: Sarah

Primary Readings

Descartes, "Third Meditation"
Descartes, "Fifth Meditation"
Leibniz, "Meditations on Knowledge, Truth, and Ideas"

Secondary Readings

Kline, "The Mathematization of Science"
Kline, "The Creation of the Calculus"

Class 6: Modern rationalism II (2/6)

Seminar Paper: Kara

Primary Readings

Locke, *Essay*, Bk 1, Ch. 1
Leibniz, Selections from *New Essays*

Class 7: Modern empiricism (2/11)

Seminar Paper 1: James

Seminar Paper 2: Katherine

Primary Readings

Selections from Berkeley's *Principles*

Selections from Hume on Mathematics

Class 8: The synthetic a priori I (2/13)

Seminar Paper: Nelson

Primary Readings

Selections from Kant's *Critique*

Kant, *Prolegomena*, §§1-2

Secondary Reading

Shapiro, pp 76-91

Class 9: The synthetic a priori II (2/18)

Seminar Paper: Heather

Readings

See Readings for Class 8

Class 10: Radical empiricism (2/20)

Seminar Paper: Jonathan

Primary Readings

Mill, *System of Logic*, Book II, §V and §VI

Frege, *Foundations of Arithmetic*, §7-§10

Secondary Readings

Shapiro, pp 91-102

Class 11: Cantor's Paradise (2/25)

Seminar Paper: Walter

Primary Reading

Tiles, "Cantor's Transfinite Paradise"

Secondary Readings

Dauben, "Cantor's Philosophy of the Infinite"

Tiles, "Numbering the Continuum"

Class 12: Logicism (2/27)

Seminar Paper: Kara

Primary Readings

Frege, from *The Foundations of Arithmetic*, II

Russell, "Letter to Frege"

Frege, "Letter to Russell"

Secondary Readings

Russell, "On Our Knowledge of General Principles"

Russell, "How *A Priori* Knowledge is Possible"

Shapiro, pp 107-115

Class 13: Formalism (3/3)

Seminar Paper: Matt

Primary Readings

Hilbert, "On the Infinite"

Secondary Readings

Brown, pp 62-71

Shapiro, pp 140-165

Class 14: Incompleteness (3/5)

Seminar Paper: James

Primary Readings

Johann von Neumann, "The Formalist Foundations of Mathematics"

Smullyan, "The General Idea Behind Gödel's Proof"

Secondary Readings

Shapiro, pp 165-168

Class 15: Intuitionism (3/10)

Seminar Paper: Katherine

Primary Readings

Heyting, "Disputation"

Brouwer, "Intuitionism and Formalism"

Brouwer, "Consciousness, Philosophy, and Mathematics"

Secondary Readings

Brown, Chapter 8

Shapiro, pp 172-189

Class 16: Carnap (3/12)

Seminar Paper: Heather

Primary Readings

Carnap, "Empiricism, Semantics and Ontology"

Secondary Reading

Shapiro, pp 124-133

Class 17: Wittgenstein's Conventionalism (3/31)

Seminar Paper: Matt

Primary Readings

Wittgenstein, Selections from *Remarks on the Foundations of Mathematics*

Secondary Reading

Brown, Chapter 9

Class 18: Wittgenstein's Conventionalism (4/2)

Seminar Paper: Jazmine

Primary Readings

See Class 17, plus...

Ayer, "The A Priori"

Class 19: Gödel platonism (4/7)

Seminar Paper: Sarah

Primary Reading

Gödel, "What is Cantor's Continuum Problem? (1964)"

Secondary Readings

Shapiro, pp 201-212

Feferman, et al., "Introductory Note..."

Gödel, "What is Cantor's Continuum Problem? (1947)"

Class 20: The Problem (4/9)

Seminar Paper:

Primary Readings

Benacerraf, "Mathematical Truth"

Field, "Knowledge of Mathematical Entities"

Secondary Reading

Shapiro, pp 29-39

Class 21: Quine I (4/14)

Seminar Paper:

Primary Readings

Quine, "Existence and Quantification"

Quine, "On What There Is"

Secondary Readings

Shapiro, pp 212-220

Quine, "Two Dogmas of Empiricism"

Grice and Strawson, "In Defense of a Dogma"

Class 22: Quine II (4/16)

Seminar Paper:

Primary Readings

Marcus, "Quine's Indispensability Argument"

Marcus, "Problems with Quine's Indispensability Argument"

Class 23: Structuralism I (4/21)

Seminar Paper:

Primary Reading

Benacerraf, "What Numbers Could Not Be"

Secondary Reading

Shapiro, pp 257-275

Class 24: Structuralism II (4/23)

Seminar Paper:

Primary Reading

Shapiro, "Structure"

Secondary Reading

Shapiro, pp 275-289

Class 25: Fictionalism (4/28)

Seminar Paper:

Primary Reading

Field, "Introduction: Fictionalism, Epistemology, and Modality"

Secondary Reading

Shapiro, pp 226-237

Class 26: Contemporary Platonism (4/30)

Seminar Paper 1:

Seminar Paper 2:

Primary Readings

Katz, "Conclusion: The Problems of Philosophy"

Katz, "The Epistemic Challenge to Realism"

Katz, "Toward a Realistic Rationalism"

Balaguer, "A New Platonist Epistemology"

Class 27: Modalism (5/5)

Seminar Paper 1:

Seminar Paper 2:

Primary Readings

Putnam, "Mathematics without Foundations"

Chihara, "The Constructibility Theory"

Secondary Readings

Shapiro, pp 237-243

Class 28: Computer Proofs (5/7)

Seminar Paper:

Primary Readings

Thomas Tymoczko, "The Four-Color Theorem and its Philosophical Significance."

Secondary Readings

Brown, pp 154-158

Epitaph: Hilary Putnam, "Philosophy of Mathematics: Why Nothing Works"