Philosophy 405: Knowledge, Truth and Mathematics Russell Marcus Hamilton College rmarcus1@hamilton.edu

## Reading Guide #14 - The Problem Benacerraf, "Mathematical Truth" Field, "Knowledge of Mathematical Entities"

## Benacerraf

- 1. How are concerns about semantics and epistemology central to discussions of mathematical truth? How are they in tension?
- 2. What is the standard semantic account of mathematical sentences?
- 3. How did Hilbert's project reject a standard semantics for mathematics?
- 4. What are combinatorial accounts of mathematical truth? How do they differ from platonism?
- 5. What is Benacerraf's first requirement for a theory of mathematical truth? How does it lead to Tarski's theory of truth? What are the consequences for combinatorial views?
- 6. What is Benacerraf's second requirement for a theory of mathematical truth? Which types of views fulfill this requirement best? What's wrong with them?
- 7. What is the standard view of mathematics?
- 8. What are the consequences of analyzing mathematics non-referentially? How is this a problem for combinatorialists?
- 9. What are the grammatical advantages to the standard view? How does this affect the concept of inference?
- 10. What is the main problem with the standard view?
- 11. Describe Benacerraf's causal account of knowledge. How does he argue for it? According to the causal account, how do we know general laws?
- 12. Why does Benacerraf argue that, for X to know that p, there must be a non-innate connection between the truth conditions of p and the grounds of X's knowledge? What are the consequences of this requirement?
- 13. How does Gödel propose to account for mathematical knowledge? Why does this worry Benacerraf?
- 14. What does Benacerraf like about Gödel's account? How does this relate to his criticism of that account?
- 15. How do combinatorial views have epistemological roots?
- 16. What are conventionalist accounts of mathematics?
- 17. How does Quine argue that the justification of logical truths must come wholesale? How does this function as an argument against conventionalism?
- 18. Where does Benacerraf disagree with Quine?

## Field

- 19. What is Benacerraf's challenge to the platonist? How does that challenge rely on an unattractive epistemology? How does Field urge us to understand that challenge?
- 20. What is the access problem for platonism? Consider the example of the Nepalese villages. How does the access problem affect Gödel-platonism?
- 21. What is an indispensability argument? How might an indispensability argument help the platonist?